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Mirrors on Platonic Riemann Surfaces

Abstract Let X be a Riemann surface of genus $g > 1$ and let \mathcal{M} be a regular map on X . A reflection σ of \mathcal{M} fixes some simple closed geodesics on X , which are called the mirrors of σ . Let M be a mirror on X . Then there exist two particular conformal automorphisms of \mathcal{M} that fix M setwise and rotate it in opposite directions. These automorphisms are called the rotary automorphisms of \mathcal{M} . In this talk we present a formula for the number of mirrors on X fixed by the reflections of \mathcal{M} in terms of the orders of the rotary automorphisms and the group of automorphisms of M . We also give some applications of this formula to some well known Riemann surfaces.